

**MATH 351: RIEMANN SURFACES AND DESSINS D'ENFANTS  
HOMEWORK #3**

**Problem 3.1.** Let  $X$  be a topological surface. Let  $\phi_1 : U_1 \rightarrow V_1 \subseteq \mathbb{C}$  and  $\phi_2 : U_2 \rightarrow V_2 \subset \mathbb{C}$  be local coordinates on  $X$ . We say that  $\phi_1, \phi_2$  are *holomorphically compatible* if either  $U_1 \cap U_2 = \emptyset$  or the *transition function*  $t_{12} = \phi_2 \circ \phi_1^{-1} : V_1 \rightarrow V_2$  is holomorphic.

Suppose that  $\phi_1, \phi_2$  are holomorphically compatible. Show that the associated transition function  $t_{12}$  has nonvanishing derivative  $t'_{12}$  on its domain. Conclude that  $\phi_2, \phi_1$  are holomorphically compatible.